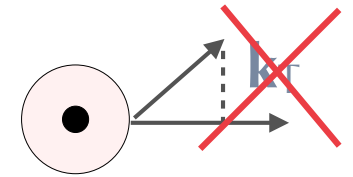
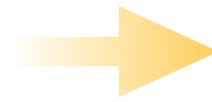


What do we know about transversity distributions of the nucleon?

Alexei Prokudin



PennState
Berks



quark polarization

nucleon polarization

| | U | L | T |
|---|----------------|-------------------|-----------------------------------|
| U | \mathbf{f}_1 | | h_1^\perp |
| L | | \mathbf{g}_{1L} | h_{1L}^\perp |
| T | f_{1T}^\perp | g_{1T} | $\mathbf{h}_1 \quad h_{1T}^\perp$ |

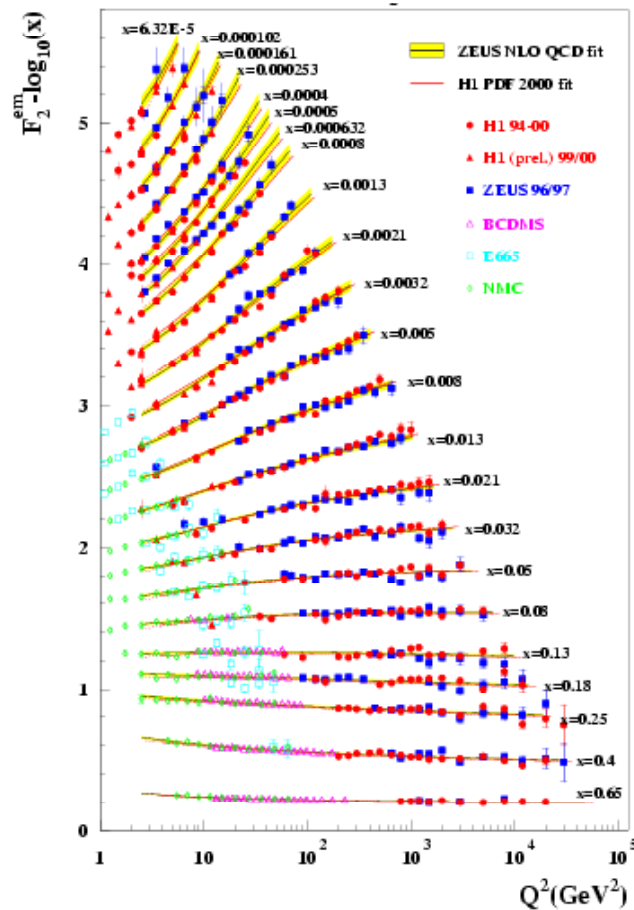
$$f_1 = \text{circle with black dot}$$

$$g_1 = \text{circle with red arrow pointing right} - \text{circle with black dot and red arrow pointing left}$$

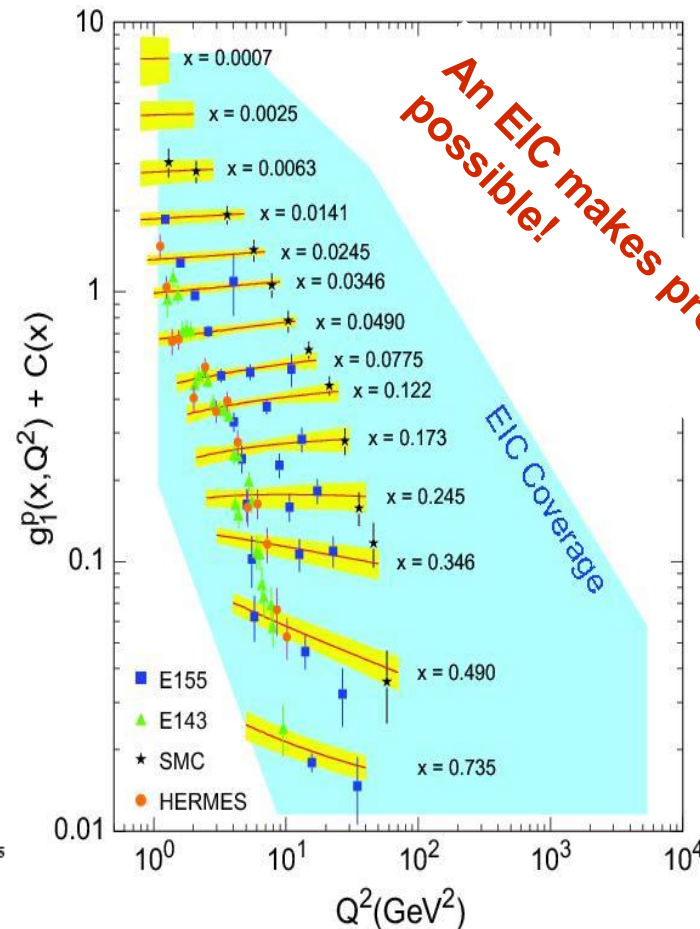
$$h_1 = \text{circle with red arrow pointing up and black dot} - \text{circle with black dot and red arrow pointing down}$$

h_1 is the transversity distribution

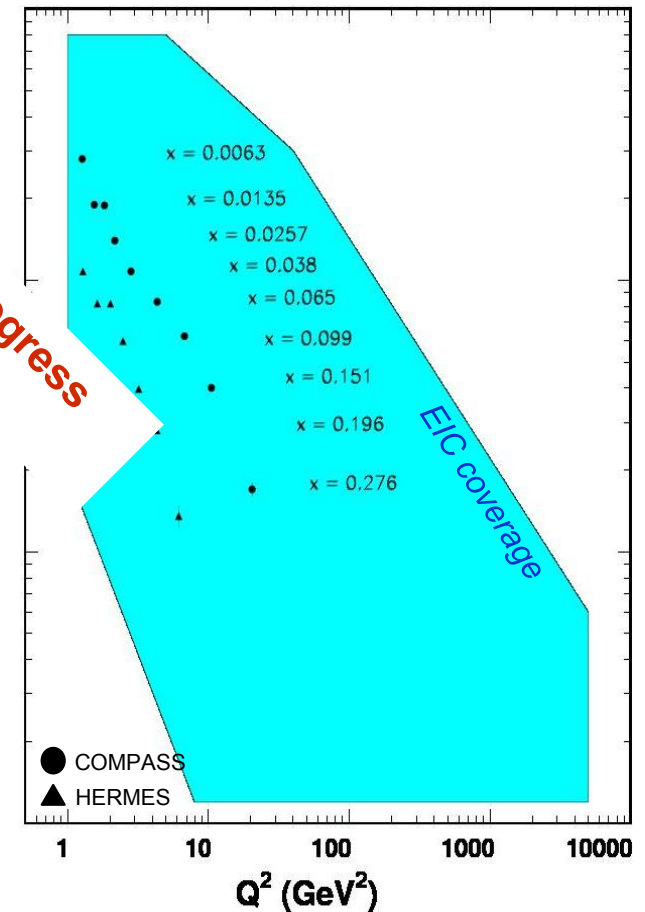
Transversity is poorly known?



World data for F_2^p
 f_1 from fits of
 thousands data



World data for g_1^p
 g_1 from fits of
 hundreds data



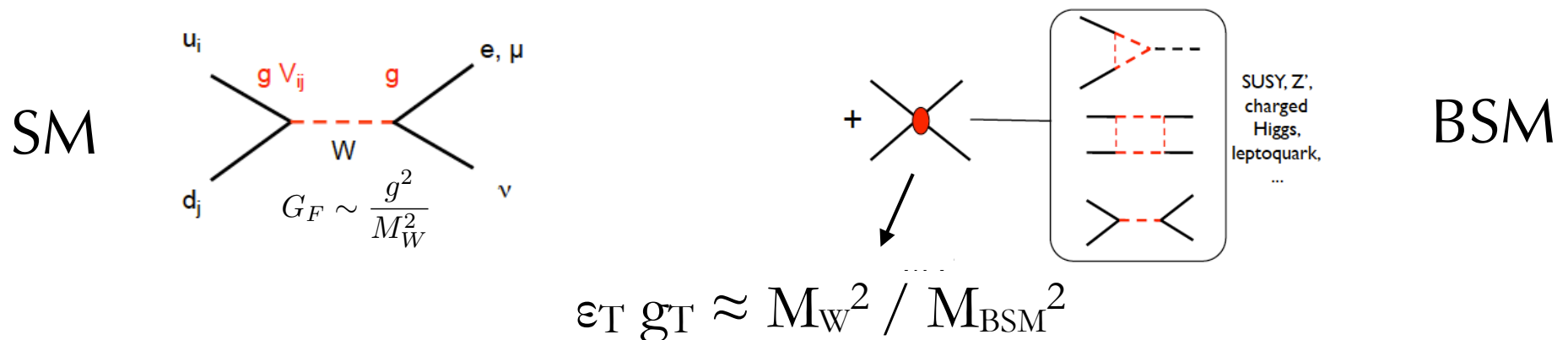
World data for h_1
 from fits of tens data

- 1st Mellin moment of transversity \Rightarrow tensor “charge”

$$\delta q \equiv g_T^q = \int_0^1 dx \left[h_1^q(x, Q^2) - h_1^{\bar{q}}(x, Q^2) \right]$$

tensor charge not directly accessible in \mathbf{L}_{SM}
 low-energy footprint of new physics at higher scales ?

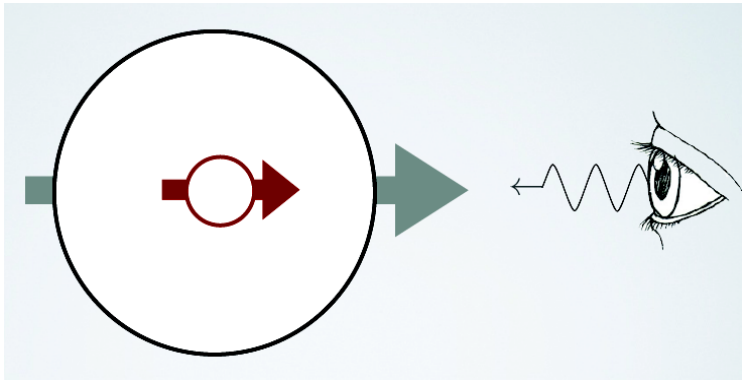
Example: neutron β -decay $n \rightarrow p e^- \bar{\nu}_e$



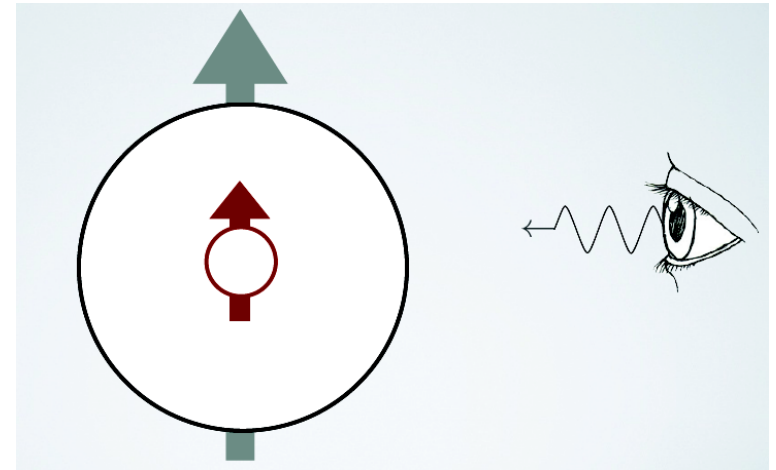
Current precision of 0.1% \Rightarrow [3-5] TeV bound for BSM scale

What did we know about transversity before
the EIC whitepaper ?

Helicity distribution

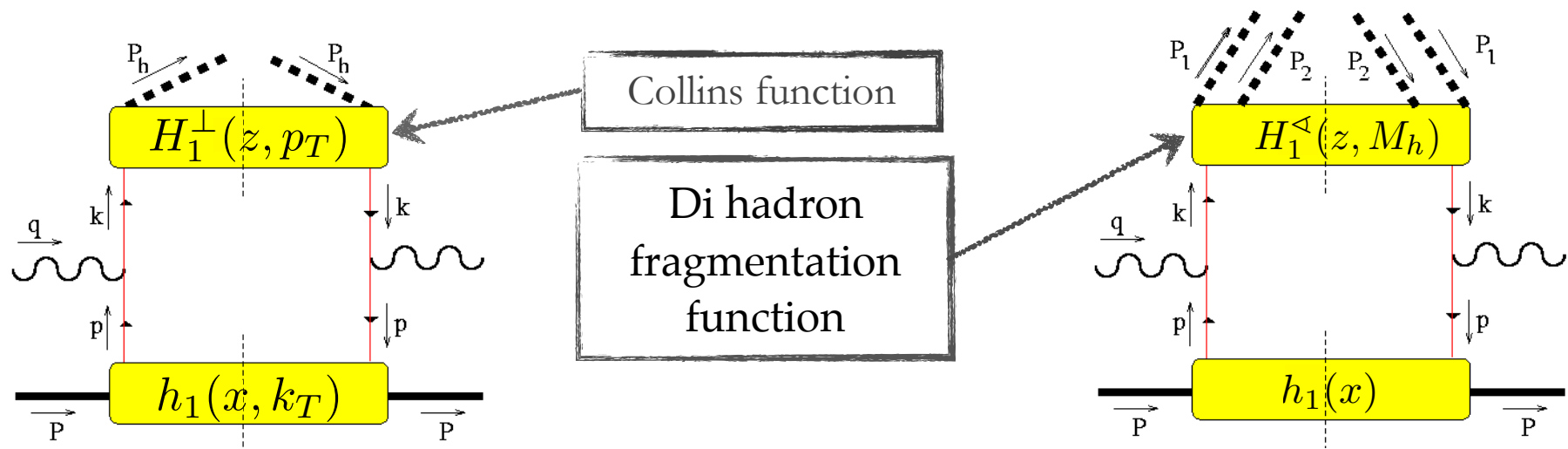


Transversity distribution



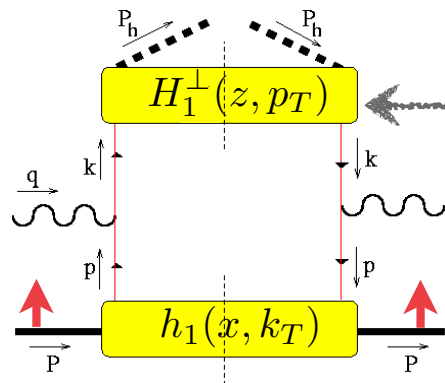
Boost and rotation do not commute \rightarrow helicity and transversity are different!

Transversity is a chiral odd quantity \rightarrow needs another chiral odd quantity to be measured in Semi Inclusive Deep Inelastic Scattering (SIDIS)



First extractions of transversity: the Collins effect

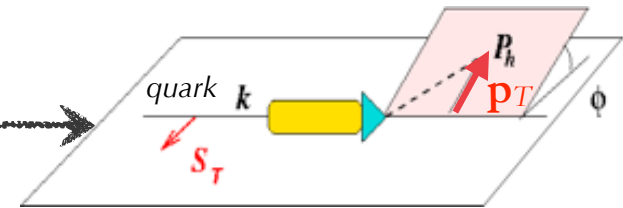
one-hadron SIDIS



Collins function

$$\sin(\phi_h + \phi_S)$$

TMD factorization

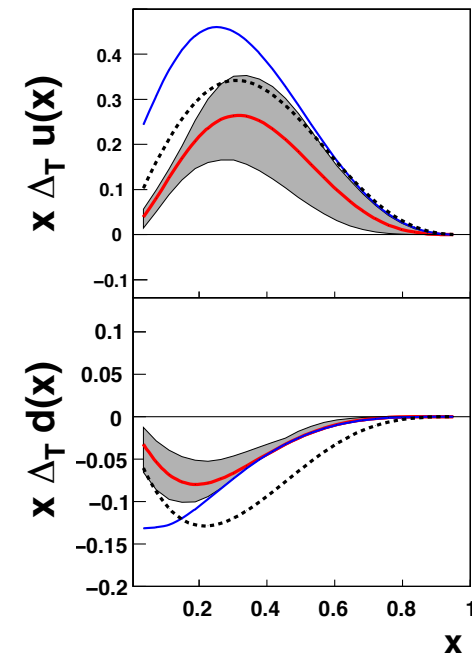


correlation \mathbf{S}_T and \mathbf{p}_T
→ azimuthal asymmetry

$$A_{\text{SIDIS}}^{\sin(\phi_h + \phi_S)}(x, z, P_T^2) \sim \frac{\sum_q e_q^2 h_1^q(x, \mathbf{k}_\perp^2) \otimes H_{1,q}^\perp(z, \mathbf{p}_\perp^2)}{\sum_q e_q^2 f_1^q(x, \mathbf{k}_\perp^2) \otimes D_{1,q}(z, \mathbf{p}_\perp^2)}$$

*Efremov et al (2005), Vogelsang, Yuan (2005),
Anselmino et al (2005,2009), Collins et al (2006)...*

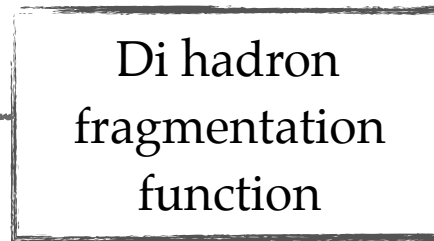
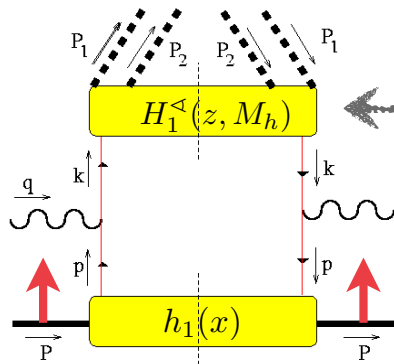
SIDIS data from  and 
e⁺e⁻ data from 



*Anselmino et al., Nucl.Phys.Proc.Suppl.
191 (2009) 98-107*

di-hadron fragmentation (DiFF)

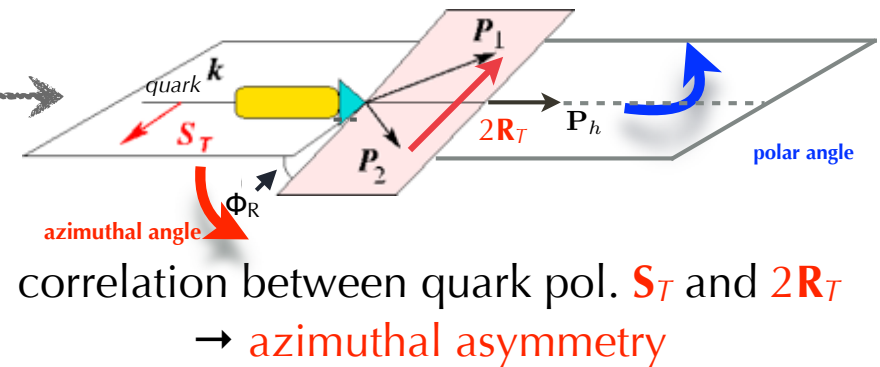
one-hadron SIDIS



$$\sin(\phi_R + \phi_S)$$

Collinear factorization

Collins, Heppelman, Ladinsky (1994)



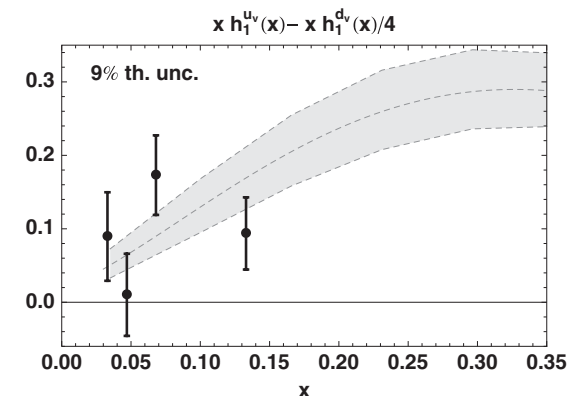
Radici, Jakob, Bianconi, (2002)

chiral-odd DiFF

$$A_{\text{SIDIS}}^{\sin(\phi_R + \phi_S)}(x, z, M_h^2) \sim - \frac{\sum_q e_q^2 h_1^q(x) \frac{|\mathbf{R}_T|}{M_h} H_{1,q}^{\leq}(z, M_h^2)}{\sum_q e_q^2 f_1^q(x) D_{1,q}(z, M_h^2)}$$

$$Z = Z_1 + Z_2$$

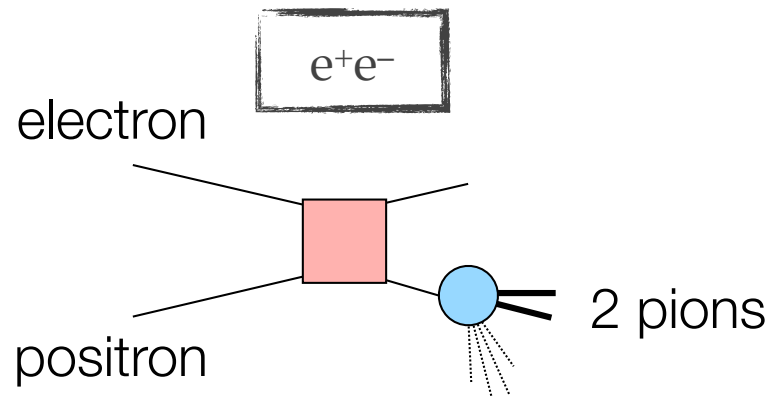
price to pay: dependence
on $(\pi\pi)$ invariant mass M_h



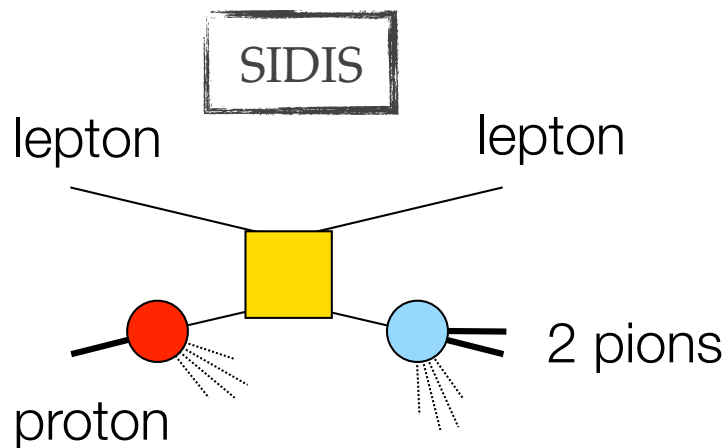
Bacchetta, Courtoy, Radici (2011)

What about factorization for other processes ?

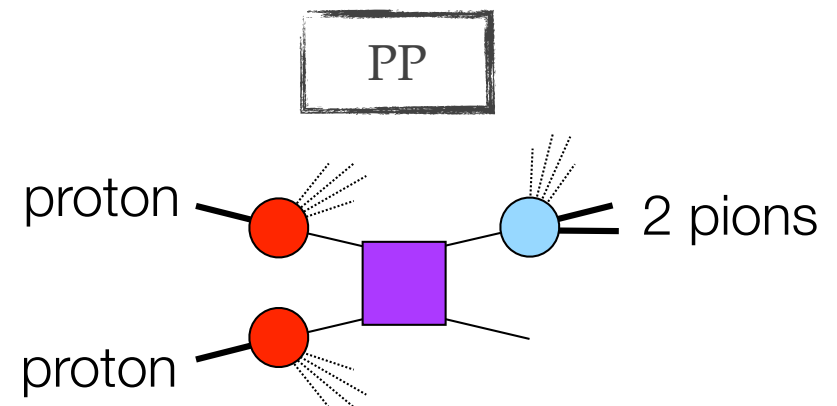
Collinear factorization for **dihadron** production



*Artru & Collins, Z.Phys. **C69** (96) 277*
*Boer, Jakob, Radici, P.R.D**67** (03) 094003*

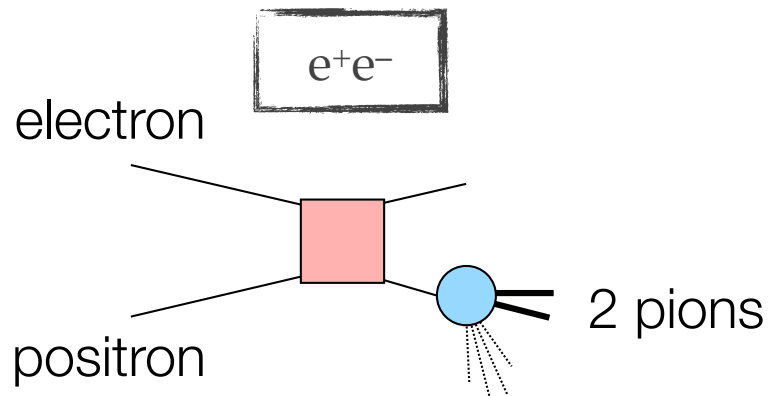


*Jaffe, Jin, Tang, P.R.L.**80** (98) 1166*
*Radici, Jakob, Bianconi, P.R.D**65** (02) 074031*
*Bacchetta & Radici, P.R. D**67** (03) 094002*

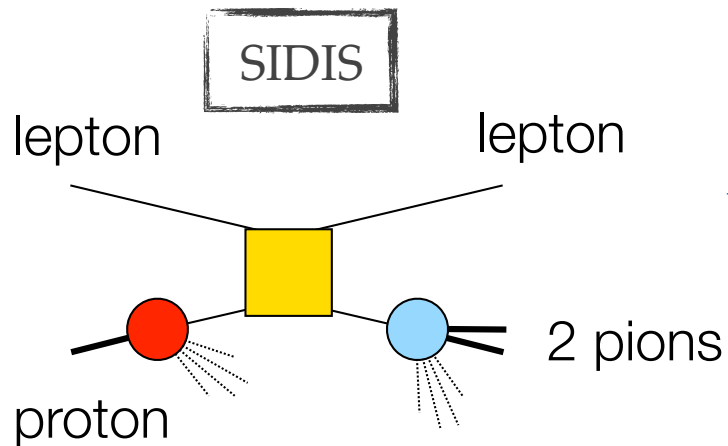


*Bacchetta & Radici, P.R. D**70** (04) 094032*

Collinear factorization for **dihadron** production



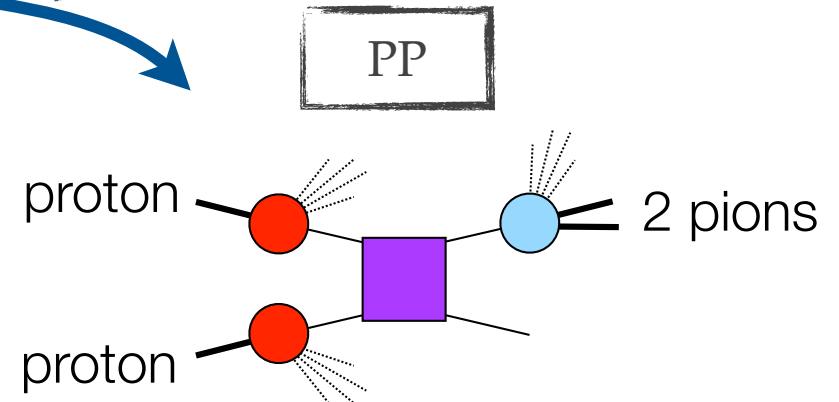
Artru & Collins, *Z.Phys.* **C69** (96) 277
Boer, Jakob, Radici, *P.R.D***67** (03) 094003



Jaffe, Jin, Tang, *P.R.L.* **80** (98) 1166
Radici, Jakob, Bianconi, *P.R.D***65** (02) 074031
Bacchetta & Radici, *P.R. D***67** (03) 094002

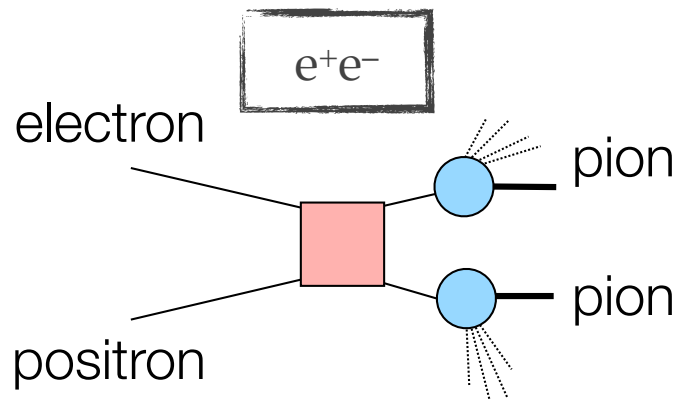
DeFlorian & Vanni, *P.L.* **B578** (04) 139
Ceccopieri, Radici, Bacchetta, *P.L.* **B650** (07) 81
Zhou and Metz, *P.R.L.* **106** (11) 172001
(M_h —evolution of DiFFs)

Standard DGLAP evolution
equations

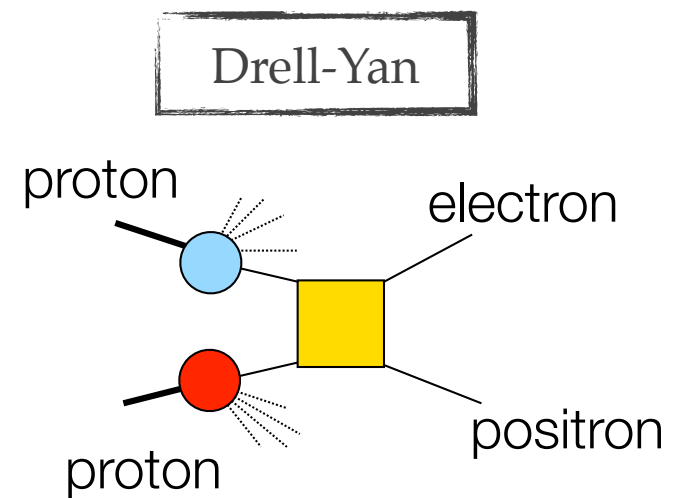


Bacchetta & Radici, *P.R. D***70** (04) 094032

TMD factorization



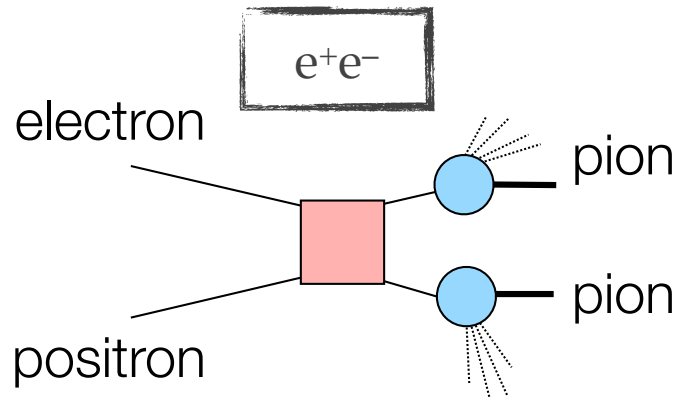
Collins, Soper, Sterman (1985)
Collins (2011)



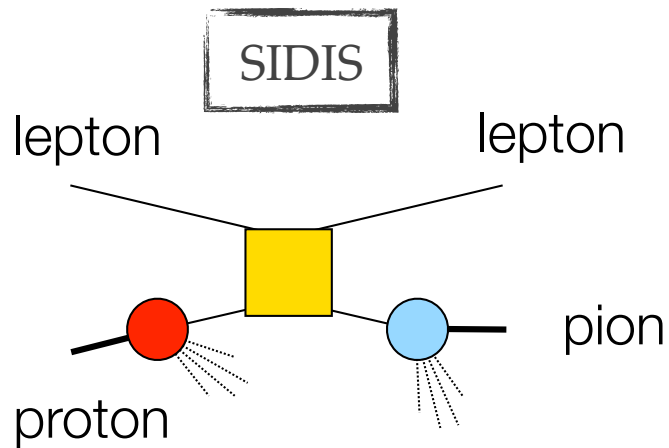
Collins, Soper, Sterman (1985)
Ji, Ma, Yuan (2004)
Collins (2011)

- TMD factorization is valid generically for processes with two measured scales $Q_1 \ll Q_2$.
- Traditionally called "resummation" by CSS for cross sections.
- Later put in the form of evolution equations for TMD functions by Collins 11.
- Complicated color flow makes it difficult to prove factorization with > 2 hadrons involved.

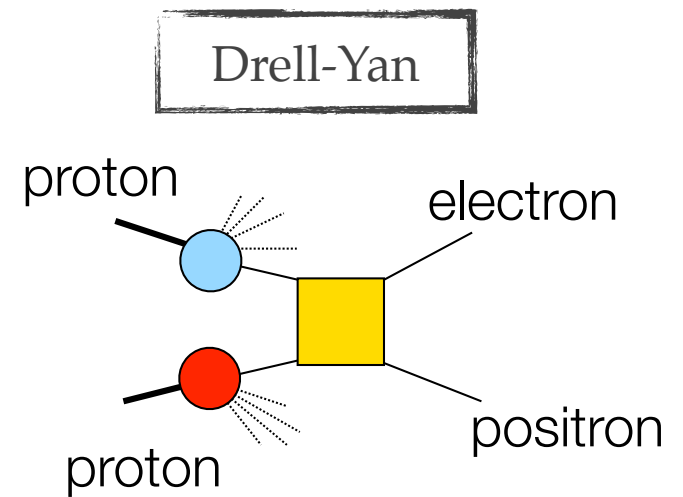
TMD factorization



Collins, Soper, Sterman (1985)
Collins (2011)

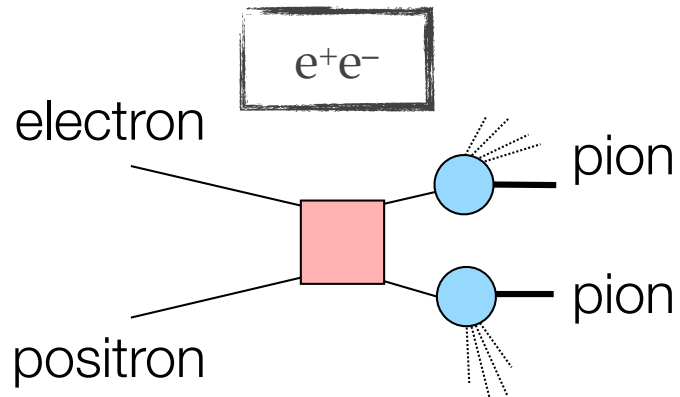


Ji, Ma, Yuan (2005)
Collins (2011)

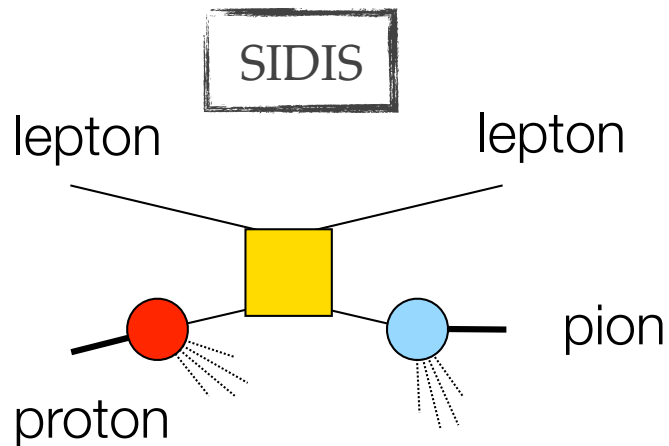


Collins, Soper, Sterman (1985)
Ji, Ma, Yuan (2004)
Collins (2011)

TMD factorization



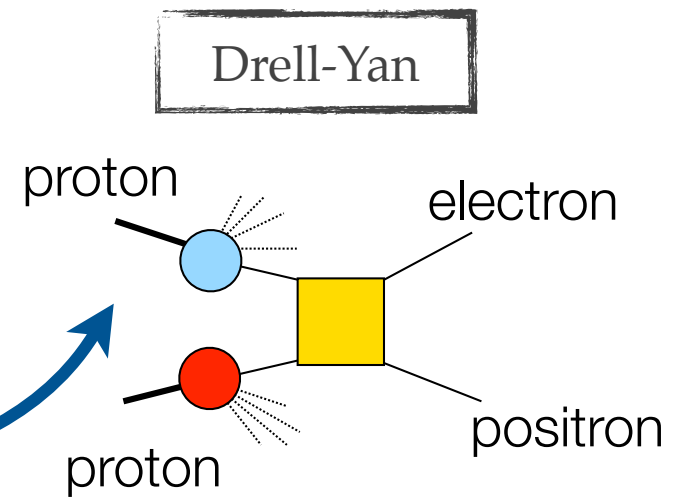
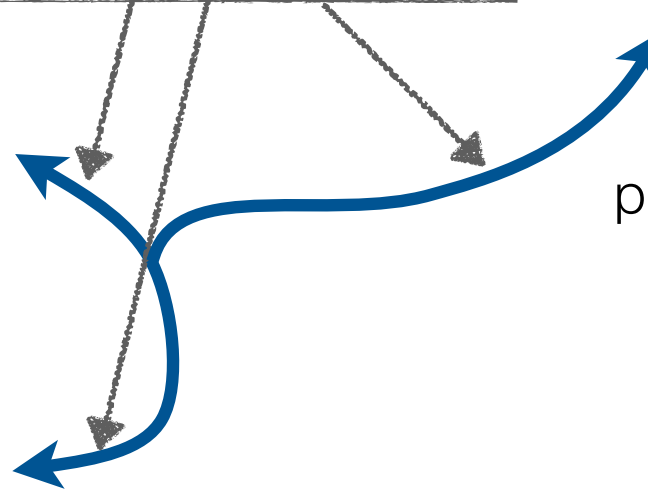
Collins, Soper, Sterman (1985)
Collins (2011)



Ji, Ma, Yuan (2005)
Collins (2011)

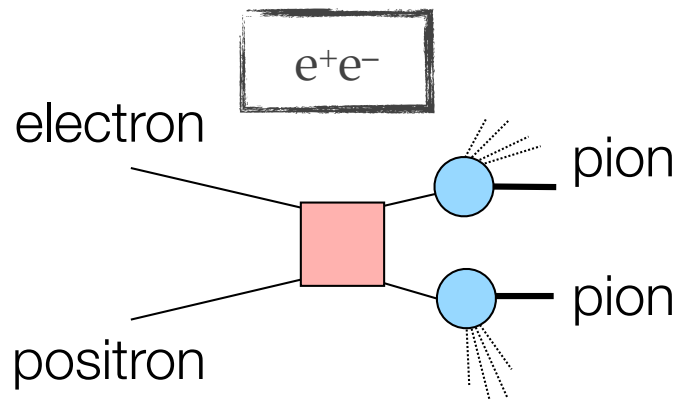
Collins, Soper, Sterman (1985)
Collins (2011)
Bacchetta, AP, (2013) for transversity

TMD evolution equations

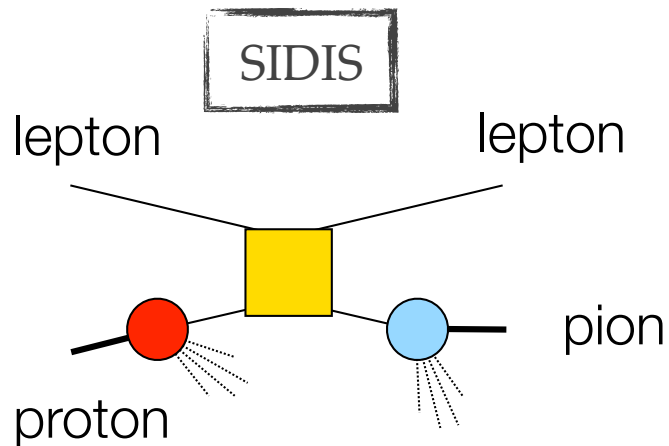


Collins, Soper, Sterman (1985)
Ji, Ma, Yuan (2004)
Collins (2011)

TMD factorization



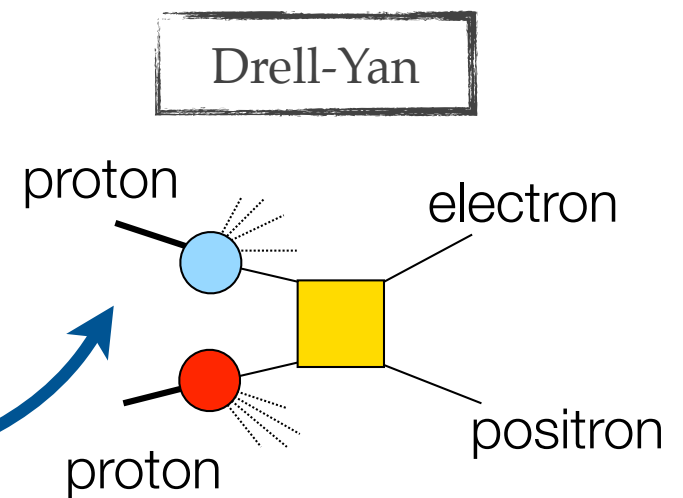
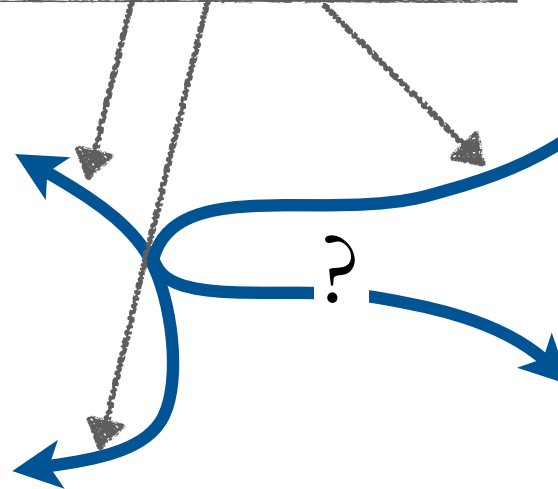
Collins, Soper, Serman (1985)
Collins (2011)



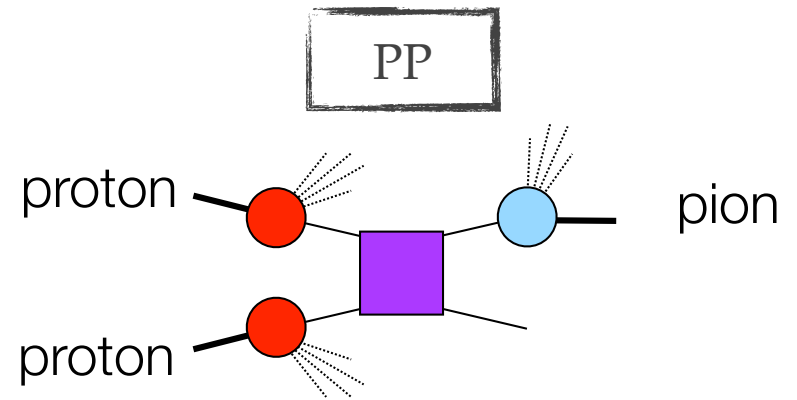
Ji, Ma, Yuan (2005)
Collins (2011)

Collins, Soper, Serman (1985)
Collins (2011)
Bacchetta, AP, (2013) for transversity

TMD evolution equations



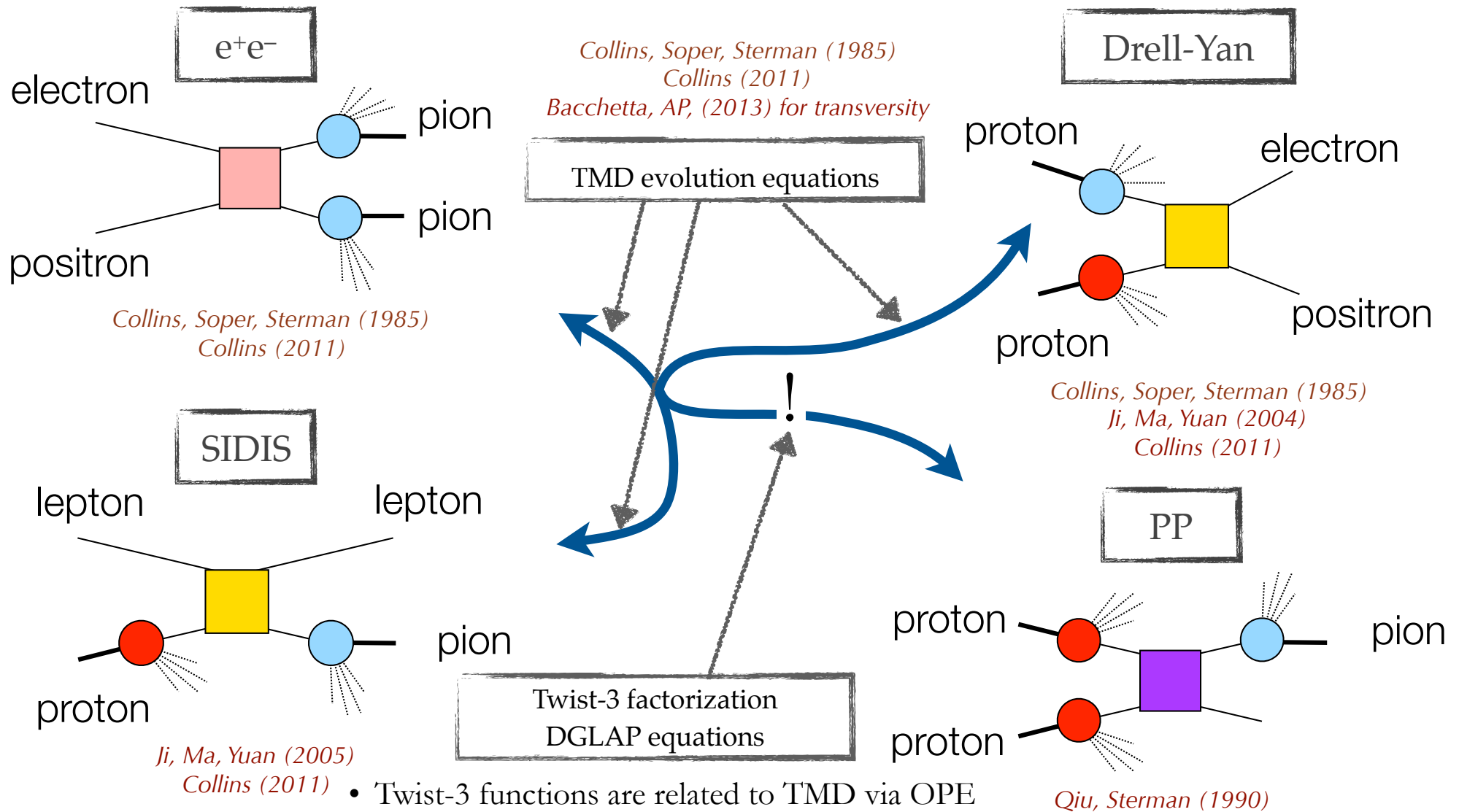
Collins, Soper, Serman (1985)
Ji, Ma, Yuan (2004)
Collins (2011)



Qiu, Serman (1990)

Only one scale is
 measured in PP
 TMD factorization is not
 applicable?

TMD factorization



- Twist-3 functions are related to TMD via OPE
- TMD and twist-3 factorizations are related in high Q^2 region
- Global analysis of TMDs and twist-3 is possible: All four processes can be used.
- Data are from HERMES, COMPASS, JLab, BaBar, Belle, RHIC, LHC, Fermilab

Global fit is needed.
Work in progress

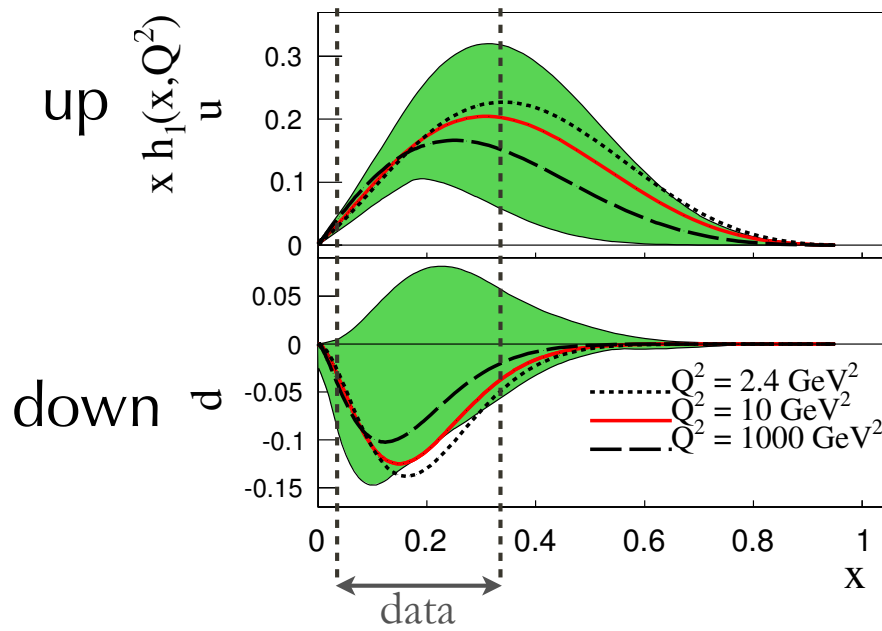
See talks by Daniel Pitonyak,
Zhongbo Kang, Nobuo Sato

What have we learnt about transversity after
the EIC whitepaper ?

TMD fits: transversity and Collins FF

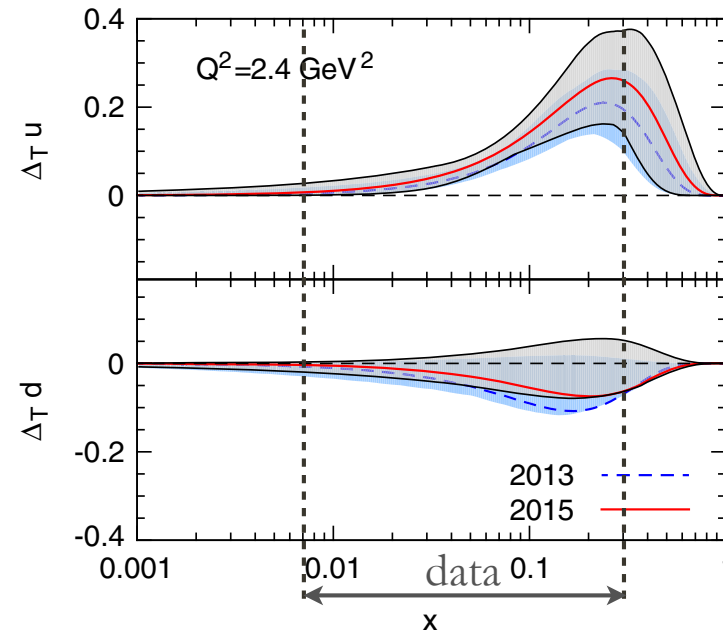
The first fit using TMD evolution

Kang et al., P.R. D93 (16) 014009



Fits without TMD evolution

Anselmino et al., P.R. D93 (15) 034025



New data:

SIDIS data from  and  and 
 e^+e^- data from  and 

History of upgrading fits:

Anselmino et al., P.R. D87 (13) 094019

Anselmino et al., P.R. D92 (15) 114023

Anselmino et al., P.R. D93 (15) 034025

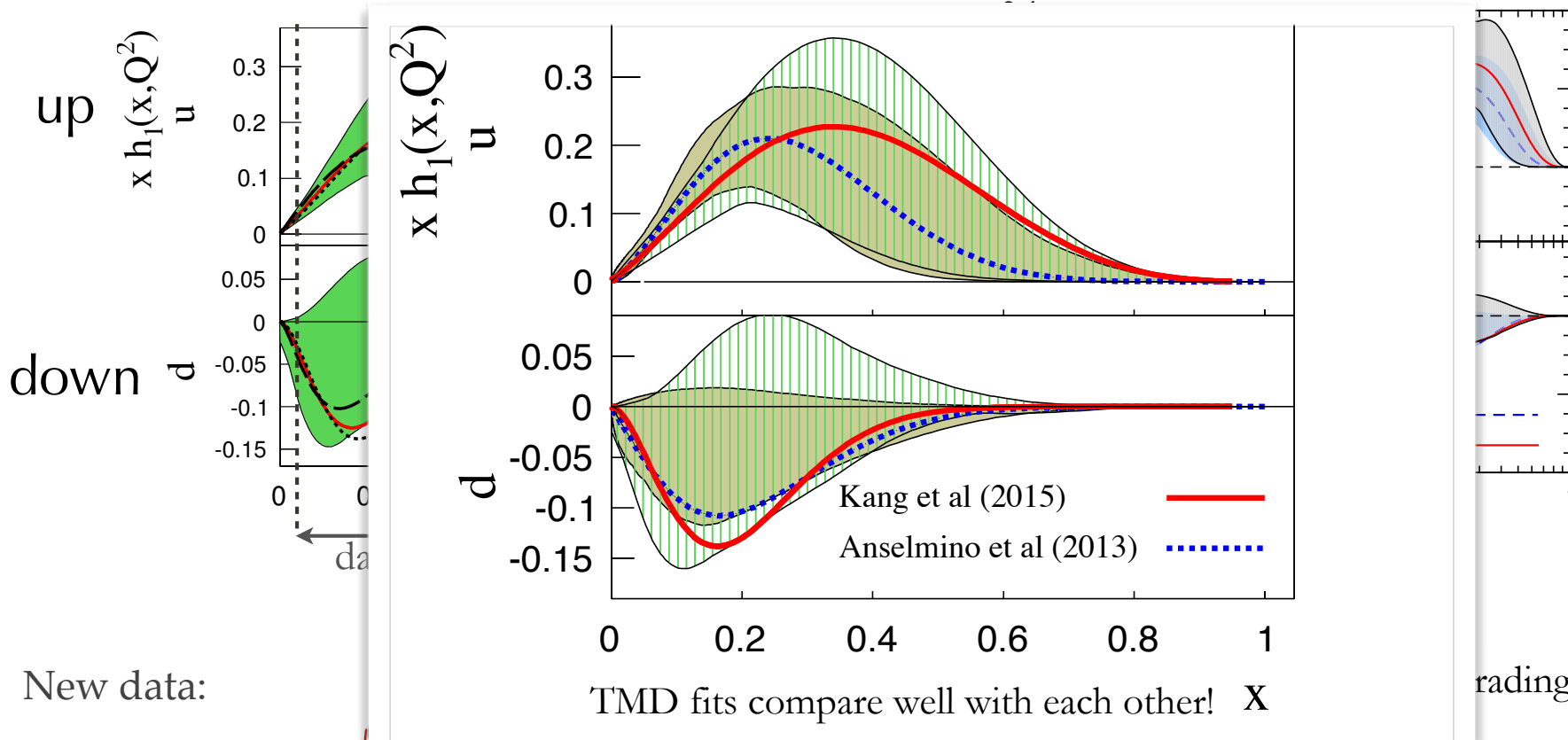
TMD fits: transversity and Collins FF

The first fit using TMD evolution

Kang et al., P.R. D93 (16) 014009

Fits without TMD evolution

Anselmino et al., P.R. D93 (15) 034025



New data:

SIDIS data from  and  and **Jefferson Lab**

Anselmino et al., P.R. D87 (13) 094019

e^+e^- data from



and



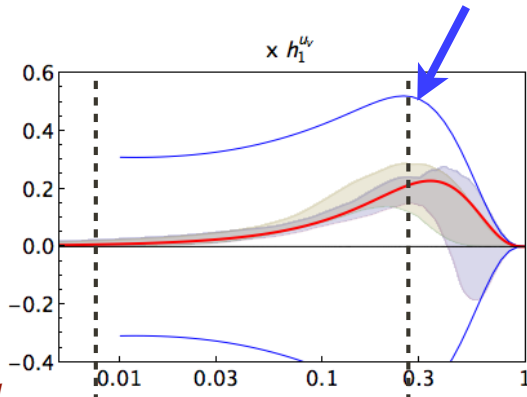
Anselmino et al., P.R. D92 (15) 114023

Anselmino et al., P.R. D93 (15) 034025

The Pavia fit: transversity and DiFF

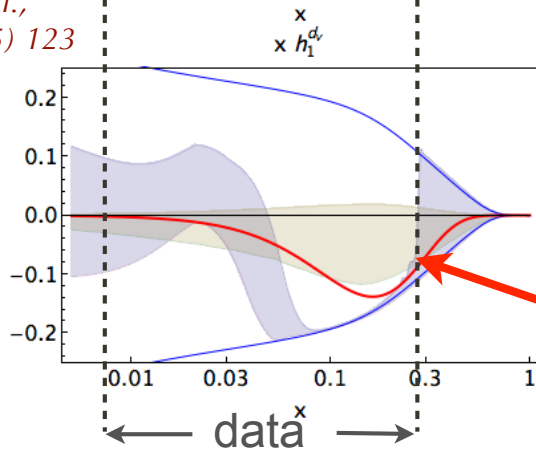
Soffer bound $2|h_1^q(x, Q^2)| \leq 2 \text{SB}_q(x) = |f_1^q(x) + g_1^q(x)|$

up



Radici et al.,
JHEP **1505** (15) 123

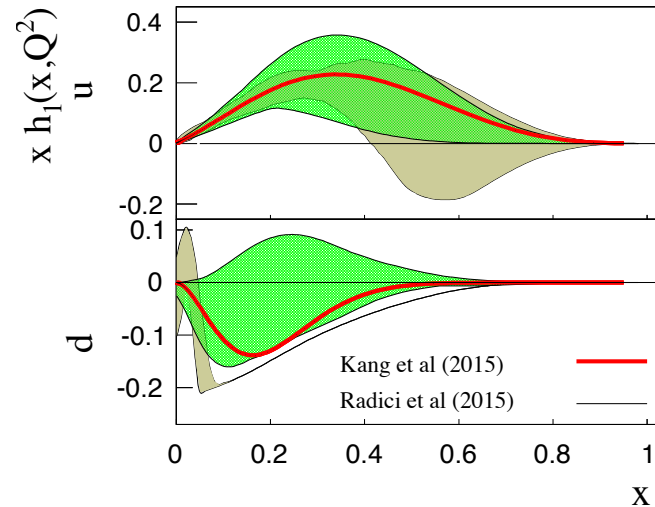
down



Anselmino et al., (2013)

Kang et al., (2015)

Kang et al. 2016 <-> Pavia 2015



$Q^2=2.4 \text{ GeV}^2$

linear
scale

New data:

SIDIS data from  and 

e^+e^- data from 

History of upgrading fits:

Bacchetta, Courtoy, Radici,
P.R.L. **107** (11) 012001

Bacchetta, Courtoy, Radici,
JHEP **1303** (13) 119

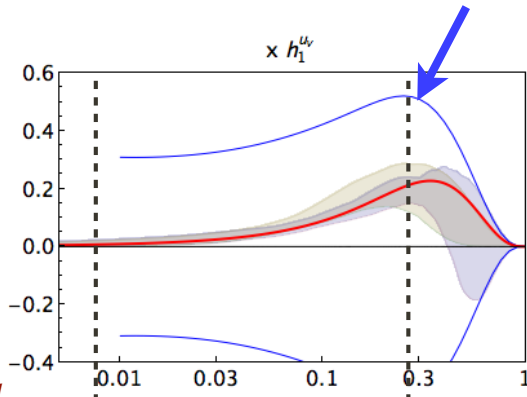
Radici et al.,
JHEP **1505** (15) 123

slide courtesy of M. Radici

The Pavia fit: transversity and DiFF

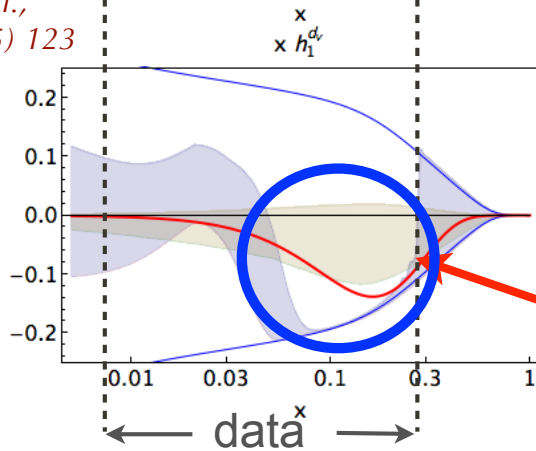
Soffer bound $2|h_1^q(x, Q^2)| \leq 2 \text{SB}_q(x) = |f_1^q(x) + g_1^q(x)|$

up



Radici et al.,
JHEP **1505** (15) 123

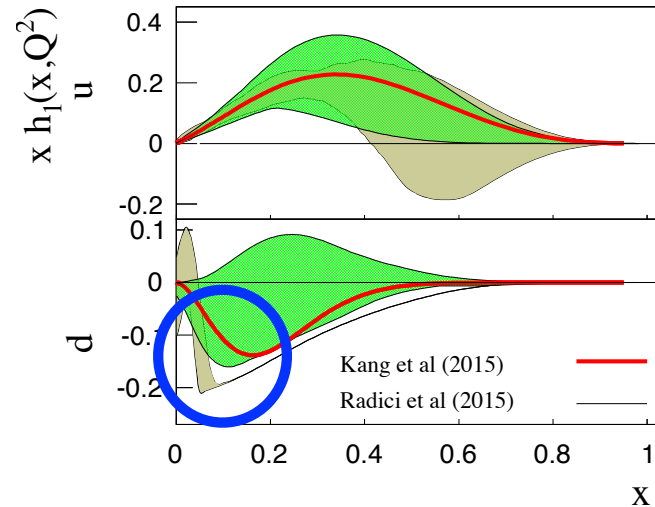
down



Anselmino et al., (2013)

Kang et al., (2015)

Kang et al. 2016 \leftrightarrow Pavia 2015





$Q^2 = 2.4 \text{ GeV}^2$

linear
scale

unusual saturation of
Soffer bound for down

New data:

SIDIS data from  and 

e^+e^- data from 

History of upgrading fits:

Bacchetta, Courtoy, Radici,
P.R.L. **107** (11) 012001

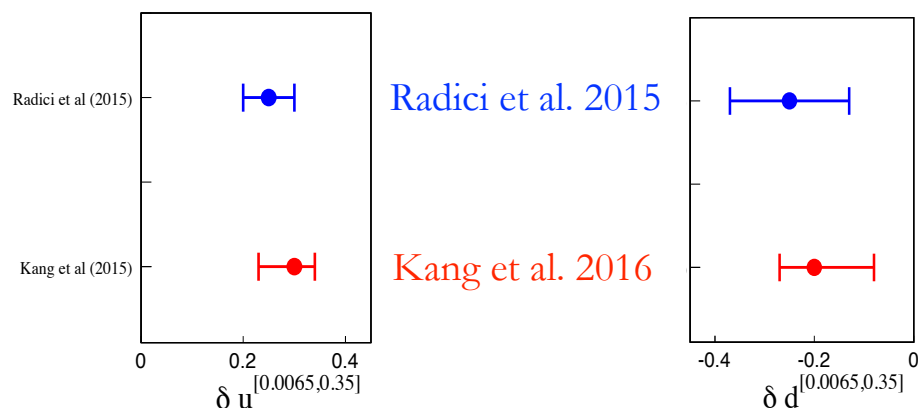
Bacchetta, Courtoy, Radici,
JHEP **1303** (13) 119

Radici et al.,
JHEP **1505** (15) 123

slide courtesy of M. Radici

$$Q^2 = 10 \text{ GeV}^2$$

$$\delta q \equiv g_T^q = \int_0^1 dx [h_1^q(x, Q^2) - h_1^{\bar{q}}(x, Q^2)]$$

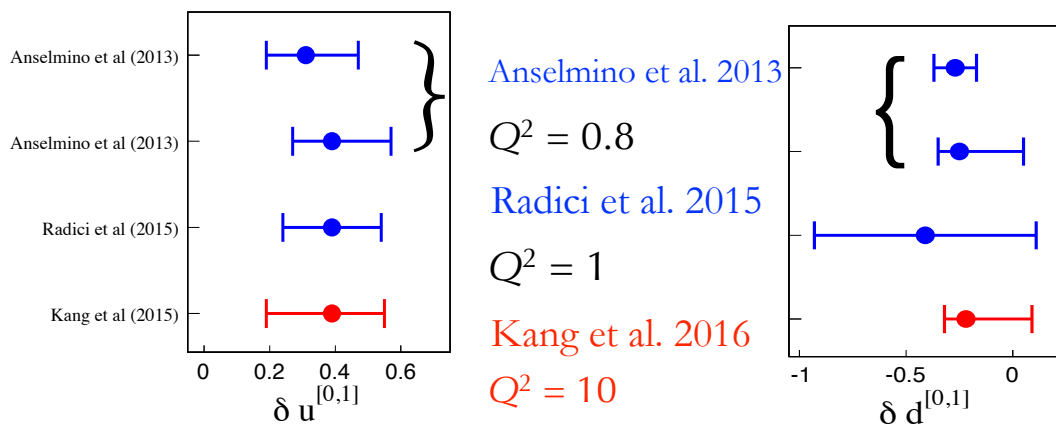


truncated to data range
 $x \in [0.0065, 0.35]$

extrapolation to $[0, 1]$



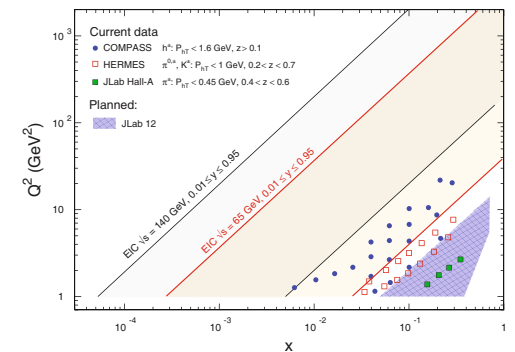
expect larger uncertainties



Data from

- Electron Ion Collider
- Jefferson Lab
- RHIC

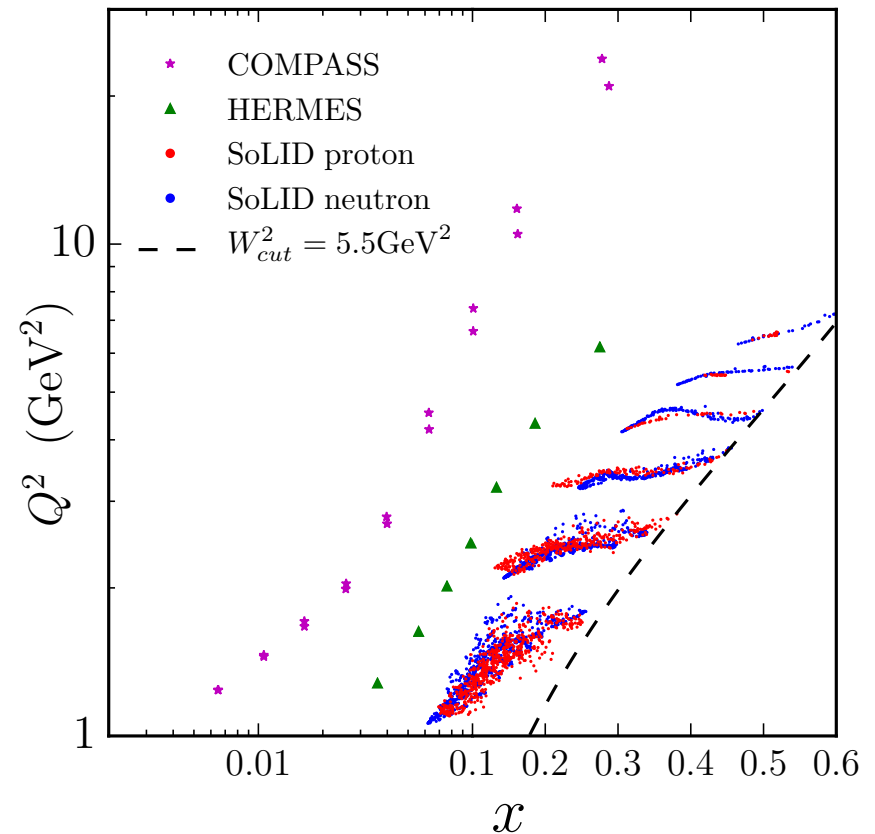
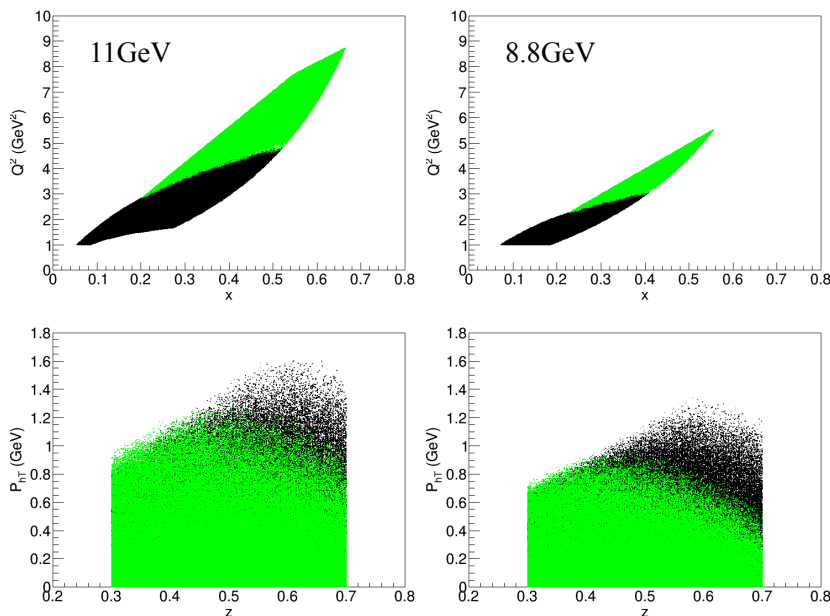
are going to reduce uncertainties



What will we learn about transversity at an EIC?

What do we expect from JLab 12?

- Electron beam: 11 GeV and 8.8 GeV
- Targets: neutron (^3He) and proton (NH_3)
- Luminosity: $\sim 10^{36} \text{ n cm}^{-2} \text{ s}^{-1}$, $10^{35} \text{ p cm}^{-2} \text{ s}^{-1}$
- Polar angle: $8^\circ \sim 24^\circ$
- Azimuthal angle: full 2π coverage
- In beam polarization: $\sim 60\%$ (^3He), $\sim 70\%$ (NH_3)
- 4D bins with high precision

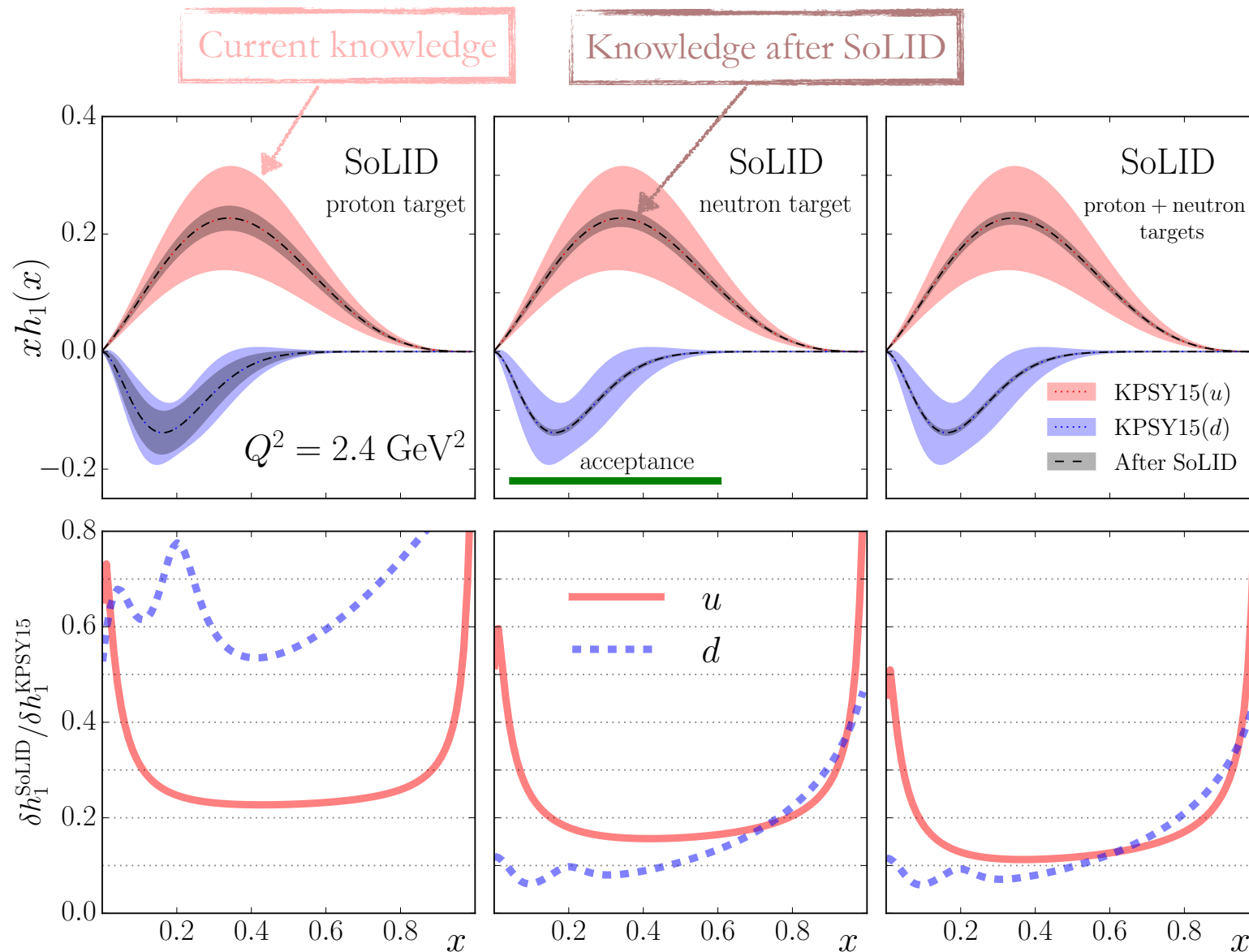


$$0.3 < z < 0.7$$

$$W' > 1.6 \text{ GeV}$$

$$Q^2 > 1.0 \text{ GeV}^2$$

What do we expect from JLab 12?

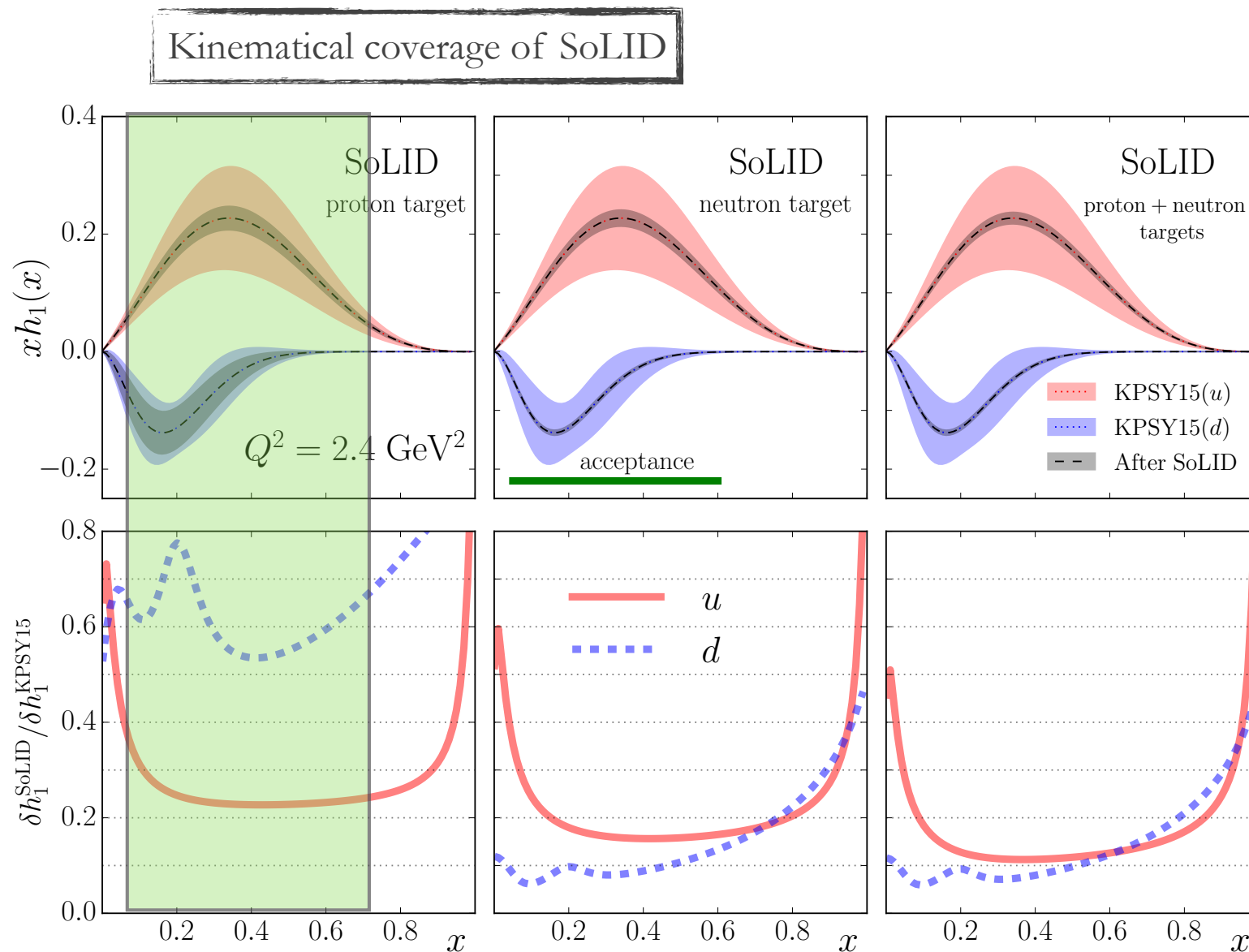


Bayesian statistics is used to estimate the improvement from new data

Current knowledge corresponds to a fit with TMD evolution *Kang et al., P.R. D93 (16) 014009*

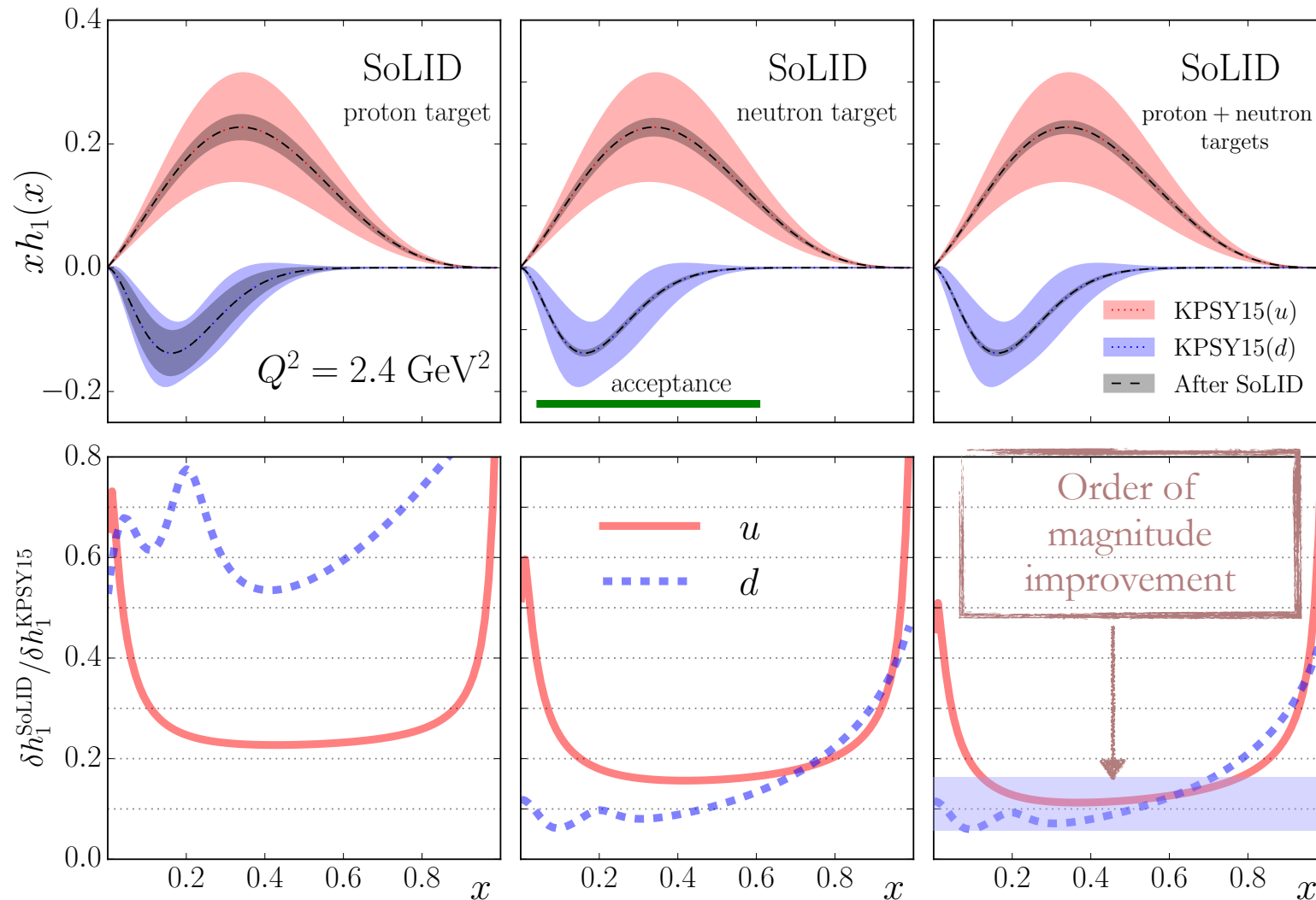
Ye et al arXiv:1609.02449 (2016)

What do we expect from JLab 12?



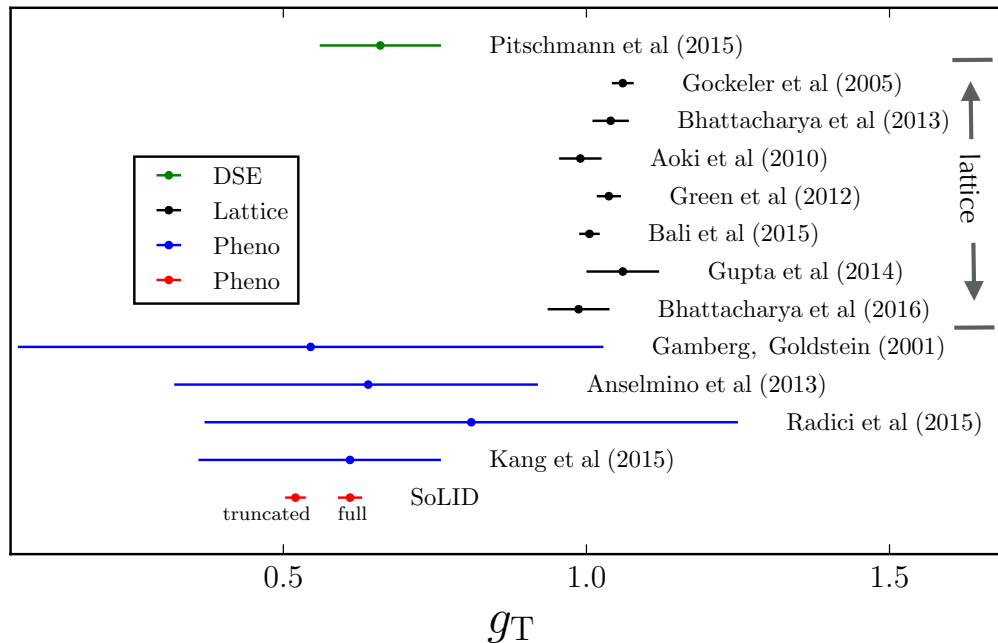
The errors grow outside of the future data region as expected

What do we expect from JLab 12?



Only combination of proton and neutron target measurements
will ensure similar improvement for both u and d quark transversities

$$g_T = \delta u - \delta d \quad \text{isovector tensor charge}$$



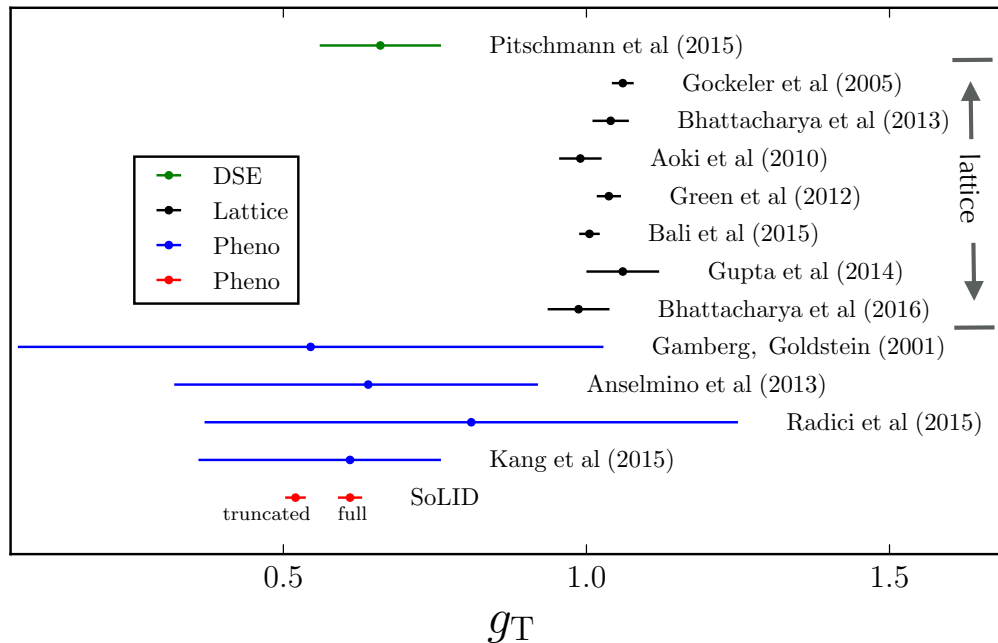
- Order of magnitude improvement is expected
- **Truncated** result is more reliable as no extrapolation is used
- Comparable with lattice QCD precision

“full” is contribution from $0 < x < 1$ region

“truncated” is contribution from $0.05 < x < 0.6$

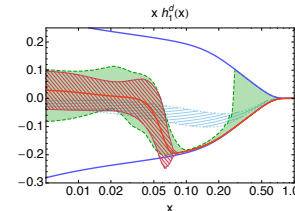
What do we expect from JLab 12?

$$g_T = \delta u - \delta d \quad \text{isovector tensor charge}$$



- Order of magnitude improvement is expected
- **Truncated** result is more reliable as no extrapolation is used
- Comparable with lattice QCD precision

- Sea quark transversity is neglected
- Extrapolation can be unreliable in the region where data are not present

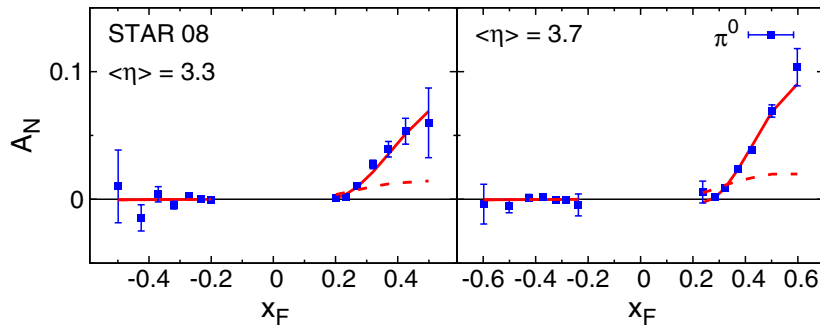


Radici et al (2015)

- Contribution from low-x region can be substantial: ~20% of tensor charge
Ye et al arXiv:1609.02449 (2016)

“full” is contribution from $0 < x < 1$ region
“truncated” is contribution from $0.05 < x < 0.6$

Twist-3 factorization, fragmentation contributions



*Kanazawa, Koike, Metz, Pitonyak
(2014)*

$$\frac{E_h d\sigma^{Frag}(S_P)}{d^3\vec{P}_h} = -\frac{4\alpha_s^2 M_h}{S} \epsilon^{P'PP_h S_P} \sum_i \sum_{a,b,c} \int_0^1 \frac{dz}{z^3} \int_0^1 dx' \int_0^1 dx \delta(\hat{s} + \hat{t} + \hat{u})$$

$$\times \frac{1}{\hat{s}(-x'\hat{t} - x\hat{u})} h_1^a(x) f_1^b(x') \left\{ \left[H_1^{\perp(1),\pi/c}(z) - z \frac{dH_1^{\perp(1),\pi/c}(z)}{dz} \right] S_{H_1^\perp}^i + \frac{1}{z} H^{\pi/c}(z) S_H^i \right.$$

$$\left. + \frac{2}{z} \int_z^\infty \frac{dz_1}{z_1^2} \frac{1}{\left(\frac{1}{z} - \frac{1}{z_1}\right)^2} \hat{H}_{FU}^{\pi/c,\mathfrak{I}}(z, z_1) S_{\hat{H}_{FU}}^i \right\},$$

Integration over \mathbf{x} for transversity, conservation of momenta in $ab \rightarrow cd$: $x_{min} = -(U/z)/(T/z + S)$

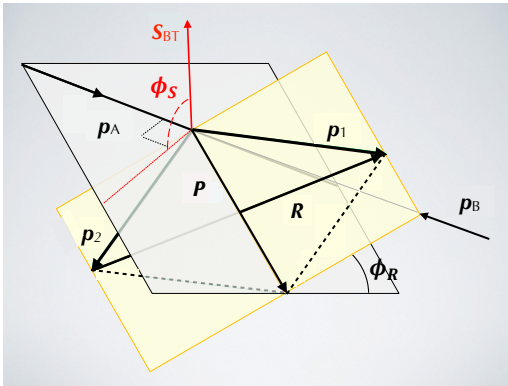
$$\int_{x_{min}}^1 \frac{dx}{x}$$

RHIC data is sensitive to high- x behavior of transversity
quark-gluon channel is dominant contribution for large x_F

More complicated structure of cross-section, additional functions to study

Improving errors in large- x
region?
Analysis in progress.

RHIC: the process $p + p^\uparrow \rightarrow (\pi \pi) + X$



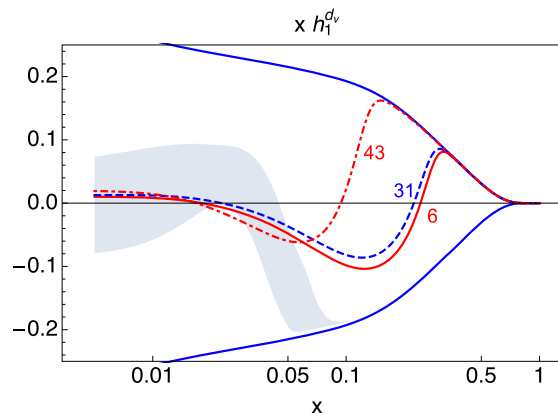
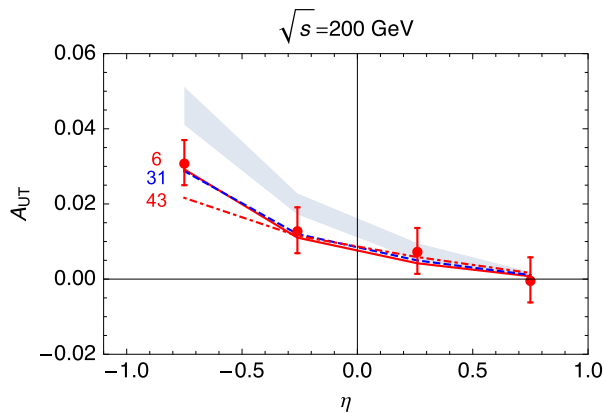
Bacchetta & Radici,
P.R. D70 (04) 094032

Assuming universality of functions for this process

$$d\sigma \sim d\sigma^0 + \sin(\Phi_S - \Phi_R) d\sigma_{UT}$$

$$A_{UT}(\eta, |P_T|, M_h) = \frac{|S_{BT}| 2|P_T| |R_T|}{d\sigma^0 M_h} \sum_{a,b,c,d} \int \frac{dx_a dx_b}{16\pi \bar{z}} \times f_1^a(x_a) h_1^b(x_b) \frac{d\Delta\hat{\sigma}_{ab\uparrow \rightarrow c\uparrow d}}{d\hat{t}} H_1^{\leq c}(\bar{z}, M_h).$$

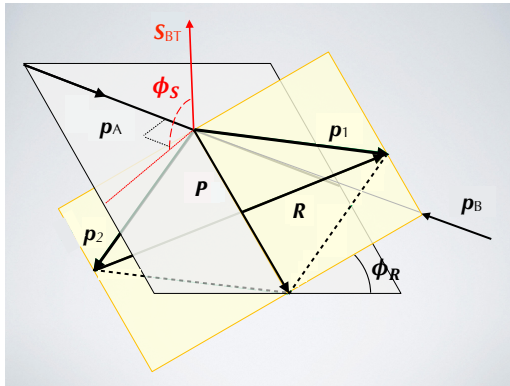
STAR data vs replicas in Pavia fit



some replicas outside the 68% band from SIDIS fit
show compatibility with p-p data in forward kinematics

Radici et al, P.R. D94 (16) 034032

RHIC: the process $p + p^\uparrow \rightarrow (\pi \pi) + X$



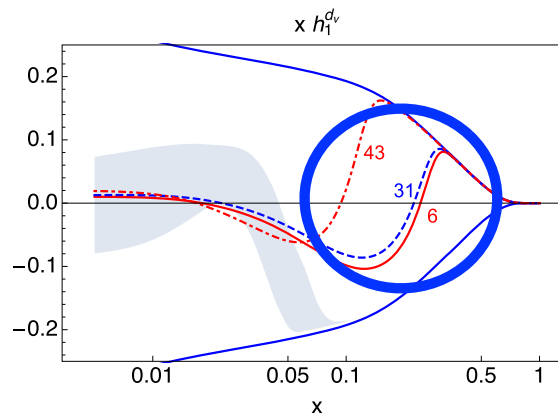
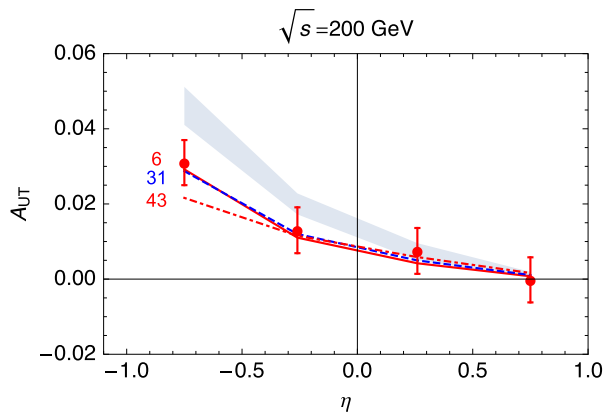
Bacchetta & Radici,
P.R. D70 (04) 094032

Assuming factorization and universality for this process

$$d\sigma \sim d\sigma^0 + \sin(\Phi_S - \Phi_R) d\sigma_{UT}$$

$$A_{UT}(\eta, |P_T|, M_h) = \frac{|S_{BT}| 2|P_T| |R_T|}{d\sigma^0 M_h} \sum_{a,b,c,d} \int \frac{dx_a dx_b}{16\pi\bar{z}} \\ \times f_1^a(x_a) h_1^b(x_b) \frac{d\Delta\hat{\sigma}_{ab\uparrow \rightarrow c\uparrow d}}{d\hat{t}} H_1^{\leq c}(\bar{z}, M_h).$$

STAR data vs replicas in Pavia fit



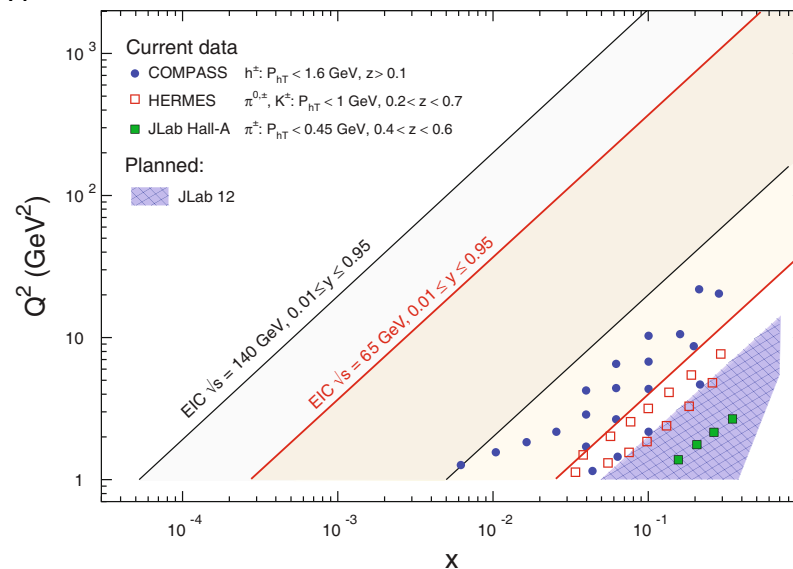
Improving errors in large-x
region?
Global fit is in progress.

some replicas outside the 68% band from SIDIS fit
show compatibility with p-p data in forward kinematics

Radici et al, P.R. D94 (16) 034032

Discussion

- ▶ Transversity can be reliably extracted using data on single and di-hadron production. Both methods are useful to check universality of functions
- ▶ Tensor charge is useful for low energy exploration of BSM physics
- ▶ Data from JLab, RHIC, EIC will complement each other as they explore different kinematical regions
- ▶ Data from Electron Ion Collider will allow
 - Extend data to low- x region
 - Explore high- Q and high- x region to complement JLab, thus explore TMD higher twist contributions



- ▶ Possible important related topics (not covered in this talk):
 - Test relationship between collinear and TMD treatment
 - Separate reliably beam and target fragmentation regions
 - Other possible ways to explore transversity using chiral-odd GPDs?
 - Lattice QCD studies as benchmark and/or constraints in fits?
 - ...

See talk by Leonard Gamberg
See talk by Osvaldo Gonzalez
Liuti, Goldstein, Courtoy, Gonzalez
See talk by Rajan Gupta